

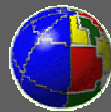


UNIVERSITA' DEGLI STUDI DI PADOVA

MECCANICA DELLA SORGENTE SISMICA: UN' INTRODUZIONE

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1. EARTHQUAKE SOURCE DYNAMICS

- Elasto – dynamic problem
- Rupture description
- Dislocation vs. crack models
- Forward modeling scheme
- Rupture stages

2. FAULT GOVERNING LAWS (CONSTITUTIVE EQUATIONS)

- Fault models
- Physical phenomena in faulting
- Fracture criteria and constitutive laws
- Strength and constitutive laws
- Slip – dependent friction laws
- Rate – and state – dependent friction laws

3. *EXAMPLES OF RUPTURE PROPAGATION IN 2 – D*

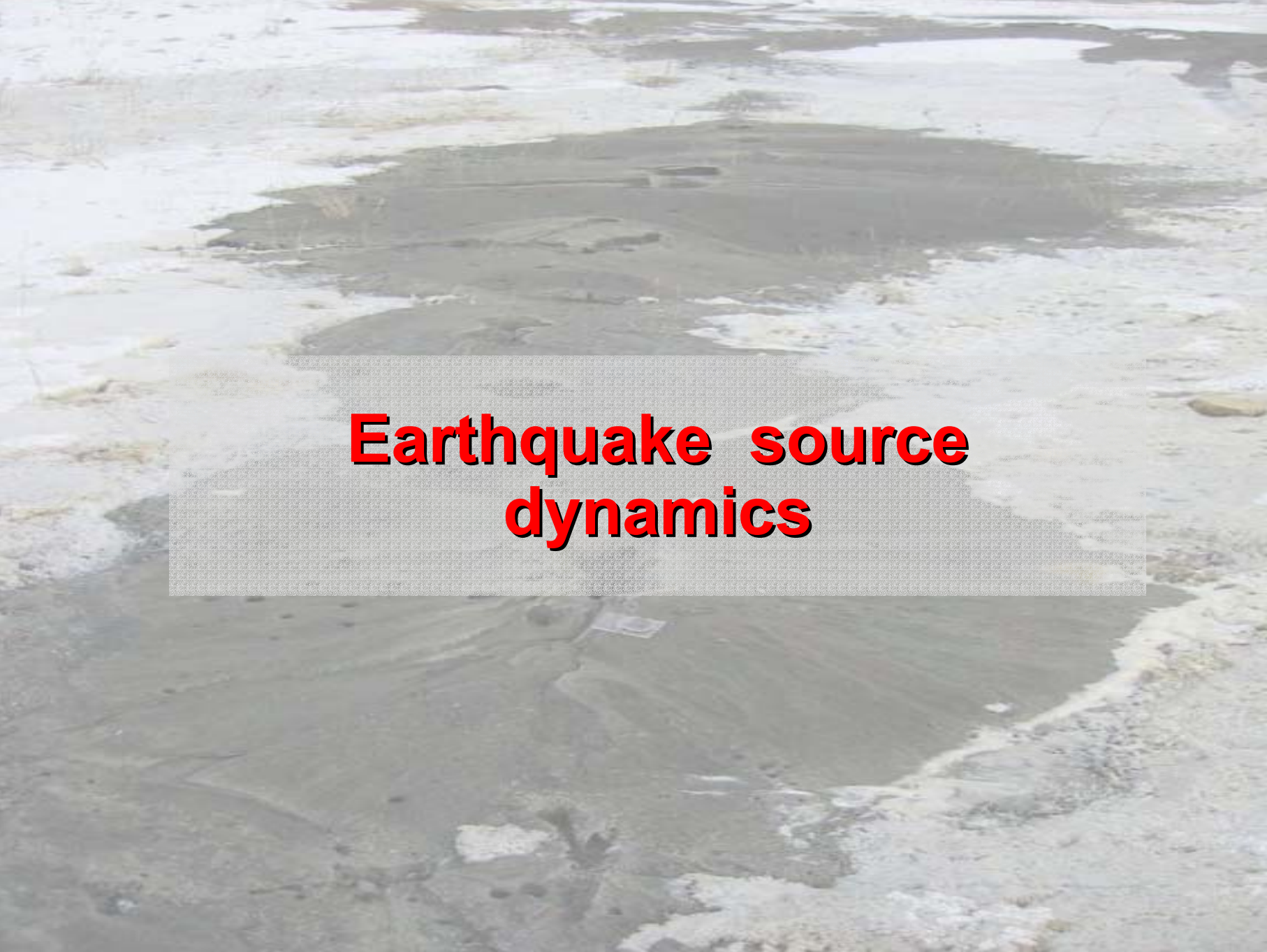
- Slip – weakening vs. Dieterich – Ruina law
- The cohesive zone and the breakdown processes
- The estimate of d_0 and related problems
- Examples of slip complexity

4. *STRESS INTERACTION AND FAULT TRIGGERING*

- Fault seismic cycle modeling
- Analytical stress perturbations
- Rhealistic stress perturbations
- Example of the 2000 South Iceland seismic sequence

Papers

1. **Belardinelli M. E., Bizzarri A., Cocco M. (2003), JGR, 108, No. B3, 2135** **BBC2003**
2. **Bizzarri A., (2003), Ph.D. Thesis** **B2003**
3. **Bizzarri A., Cocco M. (2003), JGR, 108, No. B8, 2373** **BC2003**
4. **Bizzarri A., Cocco M. (2005), Ann. Geophys., 48, No. 2, 279 - 299** **BC2005**
5. **Bizzarri A., Cocco M., Andrews D. J., Boschi E. (2003), GJI, 144, 1 – 30** **B2001**
6. **Cocco M., Bizzarri A. (2002), GRL, 29, No. 11, 11-1 – 11-4** **CB2002**
7. **Cocco M., Bizzarri A., Tinti E. (2003), Tectonophys., 378, 241 – 262** **CBT2003**
8. **Tinti E., Bizzarri A., Cocco (2005), Ann. Geophys., 48, No. 2, 327 – 345** **TBC2005**

An aerial photograph of a coastal plain or wetland area. The terrain is a mix of light-colored sand and darker, possibly water-saturated soil. A large, roughly rectangular area in the center is highlighted with a semi-transparent grey box. The text "Earthquake source dynamics" is overlaid on this box in a bold, red, sans-serif font.

Earthquake source dynamics

Elasto - dynamic problem

- * **Solution of the fundamental elasto – dynamic equation (i. e. the II law of dynamic for continuum media):**

$$\rho(d^2/dt^2)U_i = \sigma_{ij,j} + f_i \quad ; i = 1, 2, 3$$

where:

ρ is the mass cubic density,

\mathbf{U} is the particle displacement vector ($\mathbf{U} = \mathbf{x}' - \mathbf{x}$),

$\{\sigma_{ij}\}$ is the stress tensor; $\sigma_{ij} = C_{ijkl}e_{kl}$; $i,j,k,l = 1, 2, 3$, where C_{ijkl} is the elastic constant tensor, accounting for the rheology of the medium and e_{kl} is the strain tensor ($e_{kl} = 1/2 (U_{k,l} + U_{l,k})$),

\mathbf{f} is the body force vector.

- * **Choice of the dimensionality d of the problem**
($1 - D, 2 - D, 3 - D$).
($d = \text{rank of the } \mathbf{U} \text{ array, i. e. number of equations}$)

1. **Wave propagation problem: Hyperbolic PDE**
 D' Alembert wave equation:

$$\nabla^2 \mathbf{U} - (1/c_0) (\partial^2 / \partial t^2) \mathbf{U} = 0$$

where c_0 is the wave speed.

2. **Rupture propagation problem**



Rupture Description

Following *Scholz (1990)* the rupture can be described by using:

- * ***CRACK MODELS:***

The energy dissipation at crack edge (or crack tip) is paramount. Describe explicitly the crack propagation.

- * ***FRICTION MODELS:***

The effects at the edges are not explicitly considered. Explicitly allow for the calculation of the evolution of stress tensor components in terms of material properties of the fault.

Dislocation vs. Crack Models

DISLOCATION MODELS

- * Study of **displacement discontinuity**
- * **Slip** is assumed to be constant on the fault;
The fault evolution is represented by unilateral or bilateral motion (rectangular dislocations: Haskell' s model)
- * **Kinematic description:** it accounts for time evolution of rupture front and it neglects dynamics of faulting

↑ **Long period** seismic waves modeling ($\lambda \geq L_{fault}$)

↓ **constant dislocation is inadmissible;**
strain **energy** at crack tip is **unbounded;**
stress drop is infinite

CRACK MODELS

- * Impose **finite energy flow** into the rupture
- * **Slip is not prescribed**,
but it is calculated from the stress drop and from the fault strength S^{fault}
- * **Dynamic description:** the shear stress drops inside the crack (after nucleation processes), increases the stress outside the crack (near the crack tip) and tends to facilitate further grow of the rupture

↑ The motion is determined by fracture criterion (and eventually by the assumed constitutive law on the fault)

↑ The problem is characterized by assuming the boundary conditions on the fault plane. It has mixed b. c.: slip assigned outside the crack tip and stress tensor components inside the crack tip

Forward modeling scheme

1. *Fault model:*

- **Fault geometry** (orientation, planar or non – planar, ...)
- **Fault system** (multiple segments, multiple faults, ...)



2. *Medium surrounding the fault surface(s)*

- **Properties of the medium** surrounding the fault(s): cubic mass density structure, velocity structure, anisotropy, attenuation

3. *Choice of the dimensionality d' of the problem (1 – D, 2 – D, 3 – D, 4 – D).*

(d' = number of the independent variables in the solutions)



4. *Choice of the representation*

5. Choice of the numerical method

- (FE, FD, BE, BIE, SE, hybrid)

6. Specification of the Boundary Conditions

- **Domain** Boundaries Conditions (DBCs)
- **Fault** Boundary Condition (FBCs)
- **Auxiliary** Conditions (ACs)

7. Specification of the Initial Conditions

- Initial conditions **on the fault**: (initial slip, slip velocity, state variable, pre – stress);
- Initial conditions **outside the fault**: (tectonic load, (state of neighbouring faults: the fault is not an isolated system))

8. Evaluation of the solutions

- Convergence analysis (**consistency + stability**)

Rupture stages

1. Nucleation (quasi – static to dynamic evolution)

- *How can we simulate nucleation?*
- *How can we promote fault instability?*

2. Propagation

- *What is the fault constitutive equation (governing law)?*

3. Healing

- *What type of healing occurs?*
- *What controls fault healing?*

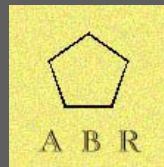
4. Rupture arrest

- *What is responsible of rupture arrest?*
- *How can we represent it? Earthquake energy balance?*

5. Fault re – strengthening

- *How can we model further instabilities episodes on the fault?*

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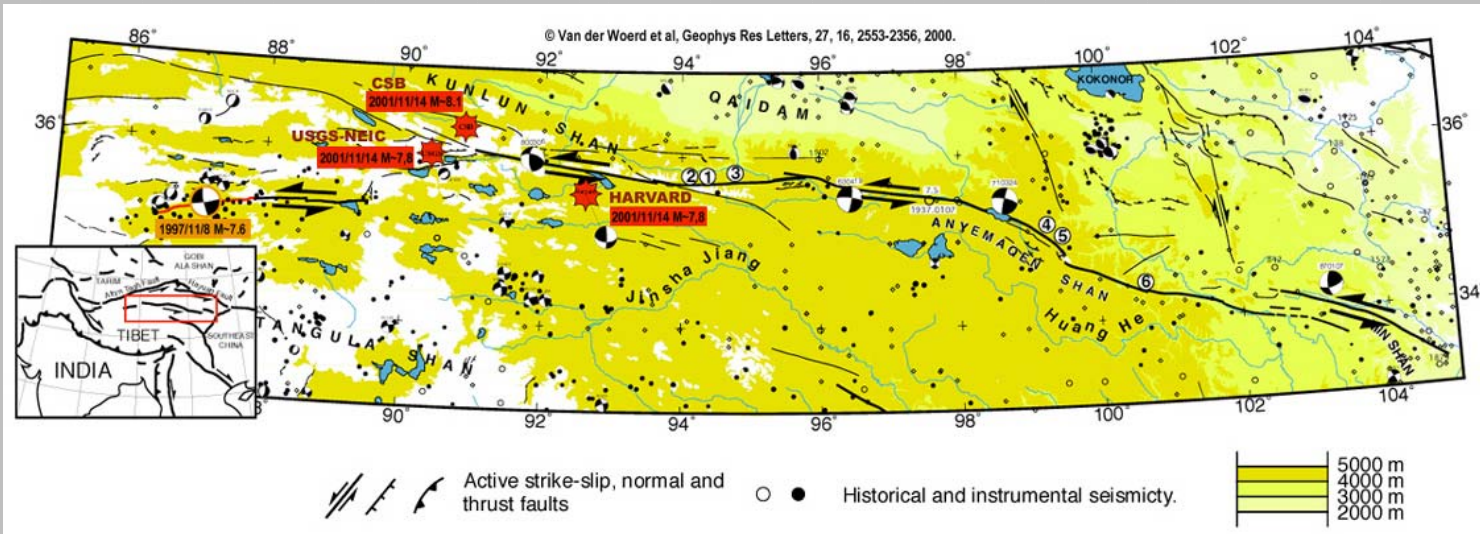
Support Slides: Parameters, Notes, etc.

To not be displayed directly. Referenced above.

Geometrical complexity

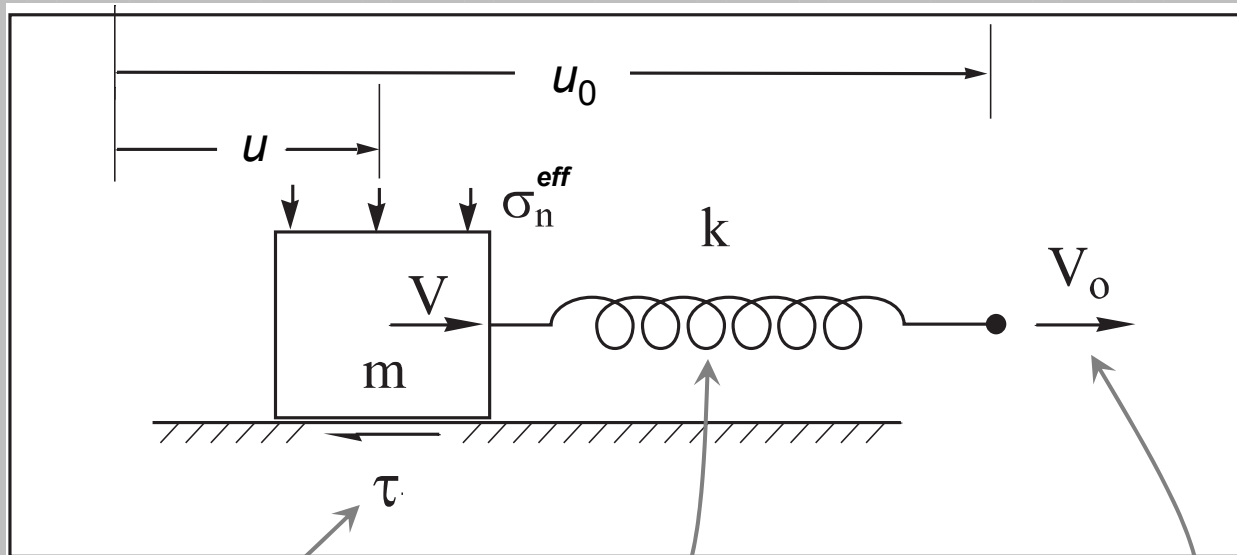


Kokoxili
 M_w 7.9
earthquake
(Qinghai
Province,
China)



Dimensionality d'

1 – D Spring – Slider (mass – spring) model



Frictional sliding

(\leftrightarrow rheological properties)

Elastic behaviour

(\leftrightarrow surrounding medium)

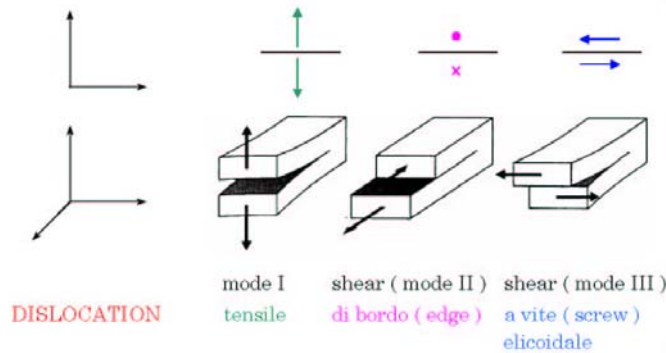
Loading velocity

(\leftrightarrow tectonic load)

Fracture propagation modes

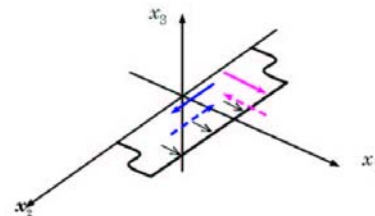
Elastodynamics Fondam. Eq.: $\rho \ddot{u}_i = f_i + \sigma_{ij,j}$

Solution: $\mathbf{u}(\mathbf{x}, t)$ (mixture of shear crack and opening crack)



Geometrical Characterization

- opening cracks (mode I) $\mathbf{u} = (0, 0, u_3(\mathbf{x}, t))$ 4 - D
- shear cracks $\mathbf{u} = (u_1(\mathbf{x}, t), u_2(\mathbf{x}, t), 0)$ 4 - D
 - Planar fault surface ($x_3 = 0$) \Rightarrow on - fault coordinates: x_1, x_3
 - $\mathbf{u} = (u_1(x_1, x_2, t), u_2(x_1, x_2, t), 0)$ truly 3 - D
 - Propagation direction: x_1

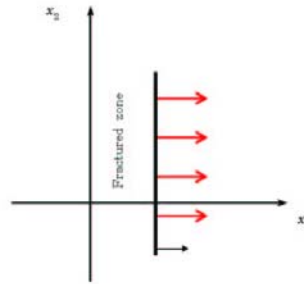


Analytical Characterization

- mixed mode $\mathbf{u} = (u_1(x_1, t), u_2(x_1, t), 0)$ pseudo 3 - D
- mode II (in - plane) $\mathbf{u} = (u_1(x_1, t), 0, 0)$ 2 - D
- mode III (anti - plane) $\mathbf{u} = (0, u_2(x_1, t), 0)$ 2 - D

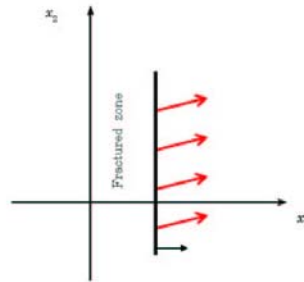
Shear rupture on a planar fault surface ($x_3 = 0$)
Snapshots at fixed time t

PURE MODE II



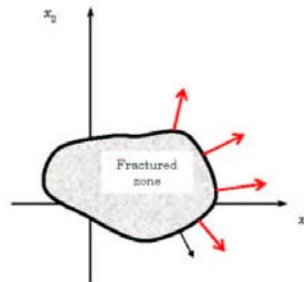
Dependence on x_1
Independence on x_2
 $\Rightarrow u_1(x_1, t)$

MIXED MODE



Dependence on x_1
Independence on x_2
 $\Rightarrow u_1(x_1, t)$
 $u_2(x_1, t)$

TRULY 3-D



Dependence on x_1
Dependence on x_2
 $\Rightarrow u_1(x_1, x_2, t)$
 $u_2(x_1, x_2, t)$

— Crack tip
— Local crack enlargement direction

→ Local displacement